

- $\hat{E}^{\dagger}\hat{E}|E\rangle = E|E\rangle$, $E \in \text{Spec}(H)$. $\langle E|\hat{E}^{\dagger}\hat{E}|E\rangle = E\langle E|E\rangle = E$

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